Using the distance based definition of a hyperbola, find the equation of the hyperbola with foci $(0, \pm 12)$ such that the distances from any point on the hyperbola to the foci differ by 4.

SCORE: / 10 PTS

$$\sqrt{x^2 + (y+12)^2} - \sqrt{x^2 + (y-12)^2} = 4$$

$$\sqrt{x^2 + (y+12)^2} = \pm 4 + \sqrt{x^2 + (y-12)^2}$$

$$\sum_{x^2 + y^2 + 24y + 144} = 16 \pm 8\sqrt{x^2 + y^2 - 24y + 144} + x^2 + y^2 - 24y + 144$$

$$48y - 16 = \pm 8\sqrt{x^2 + y^2 - 24y + 144}$$

$$6y-2=\pm\sqrt{x^2+y^2-24y+144}$$

$$36y^2 - 24y + 4 = x^2 + y^2 - 24y + 144$$

$$35y^2 - x^2 = 140$$

$$\frac{y^2}{4} - \frac{x^2}{140} = 1$$

ON PAGE 3

Convert the rectangular equation $y^2 = x^2 - 3$ to polar form. Write r as function of θ , and simplify your answer. SCORE: _____/4 PTS

$$(r\sin\theta)^2 = (r\cos\theta)^2 - 3$$

$$r^2 \sin^2 \theta = r^2 \cos^2 \theta - 3$$

$$3 = r^2 \cos^2 \theta - r^2 \sin^2 \theta$$

$$3 = r^2 \cos^2 \theta - r^2 \sin^2 \theta$$

$$3 = r^2(\cos^2\theta - \sin^2\theta)$$

$$\frac{3}{\cos^2\theta - \sin^2\theta} = r^2$$

$$\frac{3}{\cos 2\theta} = r^2 \left(\frac{1}{2}\right)$$

$$r^2 = 3\sec 2\theta$$

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SCORE: /7 PTS

A house has an exposed (straight) beam 25 feet above and parallel to the floor. A small lamp hangs from the ceiling. [a]

There is an arch such that the distance from any point on the arch to the lamp is the same as the distance from that point to the beam. The shape of the arch is a/an PARAROLA (or part of it).

- The shape of the graph of the equation $3x^2 3x + 2y^2 2y 1 = 0$ is a/an The shape of the graph of the equation $3x^2 3x + 2y^2 2y 1 = 0$ [b]
- The shape of the graph of the equation $4x^2 + 4x 3y^2 3y 1 = 0$ is a/an A = 0 is a/a [c]
- The polar co-ordinates $(-5, \frac{4\pi}{7})$ refer to the same point as the polar co-ordinates $(5, \frac{1177}{7})$. (Your answer must be **positive**.) [d]
- The polar co-ordinates $(5, \frac{4\pi}{7})$ refer to the same point as the polar co-ordinates $(5, \frac{107}{7})$. (Your answer must be <u>negative</u>.) [e]
- The point with polar co-ordinates $\left(-5, -\frac{2\pi}{3}\right)$ lies in quadrant [f]

Convert the polar equation $r^2 = \sin 2\theta$ to rectangular form.

SCORE: _____ / 4 PTS

Simplify your answer so that there are no radicals, complex fractions, fractional exponents nor negative exponents.

$$r^2 = 2\sin\theta\cos\theta$$

$$r^{2} = 2\left(\frac{y}{r}\right)\left(\frac{x}{r}\right) \quad \text{OR} \quad (r)(r)r^{2} = 2(r\sin\theta)(r\cos\theta)$$

$$r^4 = 2xy$$

$$(x^2 + y^2)^2 = 2xy$$

Find the vertices, foci and equations of the asymptotes of the hyperbola $x^2 - 3y^2 - 8x - 18y - 5 = 0$.

SCORE: ____/ 5 PTS

$$(x^2 - 8x) - 3(y^2 + 6y) = 5$$

$$(x^2 - 8x + 16) - 3(y^2 + 6y + 9) = 5 + 16 - 27$$

$$2(x^{2} - 8x + 16) - 3(y^{2} + 6y + 9) = 5 + 16 - 27$$

$$(x - 4)^{2} - 3(y + 3)^{2} = -6$$

$$\frac{(y+3)^2}{2} - \frac{(x-4)^2}{6} = 1$$

VERTICES:

$$(4, -3 \pm \sqrt{2})^{\frac{1}{2}}$$

FOCI:

$$(4, -3 \pm 2\sqrt{2})$$

ASYMPTOTES: $y+3=\pm\frac{\sqrt{3}}{3}(x-4)$

|
$$\sqrt{x^2 + (y - 12)^2} - \sqrt{x^2 + (y + 12)^2} = 44$$
 | $\sqrt{x^2 + (y - 12)^2} - \sqrt{x^2 + (y + 12)^2} = \pm 44$ | $\sqrt{x^2 + (y - 12)^2} = 24 + \sqrt{x^2 + (y + 12)^2} = \pm 44$ | $\sqrt{x^2 + (y - 12)^2} = 24 + \sqrt{x^2 + (y + 12)^2} = 244$ | $\sqrt{x^2 + (y - 12)^2} = 24 + \sqrt{x^2 + (y + 12)^2} = 244$ | $\sqrt{x^2 + (y - 12)^2} = 24 + \sqrt{x^2 + (y + 12)^2}$ | $\sqrt{x^2 + (y - 12)^2} = 24 + \sqrt{x^2 + (y + 12)^2}$ | $\sqrt{x^2 + (y - 12)^2} = 24y + 144 + x^2 + y^2 + 24y + 144$ | $\sqrt{x^2 + (y - 2)^2} = 24y + 44x + x^2 + y^2 + 24y + 144$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$ | $\sqrt{x^2 + (y + 2)^2} - \sqrt{x^2 + (y + 2)^2} = 24x$